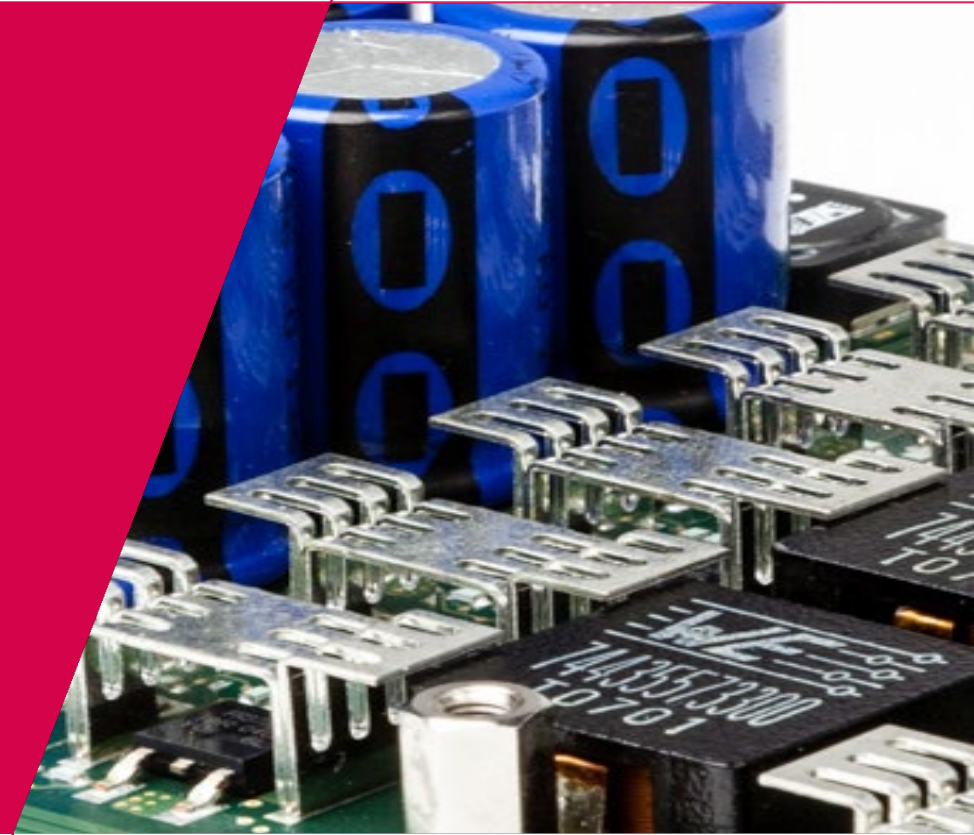


4AT060 Sustainable Vehicles (ED) 5AT010 Electrical Components

Electrical Machines

Dr. Esin Ilhan Caarls



TU / **e**

Technische Universiteit
Eindhoven
University of Technology

Where innovation starts

4AT060 & 5AT010 - 2.5ECTS

1

	Week 1	Week 2	Week 3	Week 4	Week 5	Week 6	Week 7	Week 8
3rd: 10:45-11:30	Powertrain Topologies & Modeling	Electrical Machines	Power Electronics	Charging	Batteries	Powertrain Control	Fuel Cells and Aux. Systems	Reflection
4th: 11:45-12:30								
7th: 15:45-16:30	Instructions: -Work on Assignments -Q&A					No instructions 20 th Dec.	No instructions 17 th Jan	
8th: 16:45-17:30								

Make sure you monitor CANVAS for updates etc.

ED Interim Assignment will be released today! Deadline 9 Dec!
Topics: Lecture Weeks 2-3

MENTIMETER / PULSE CHECK!

2

<https://www.menti.com/alba9o74rtep>

Go to <https://www.mentimeter.com/> → Menti Code 45 64 78 4



- **Electrical drives** (EPE courses 5XWB0 Q3, 5LWE0 Q1, 5LWH0 Q1)
- **Electrical machines (EM)** (EPE courses 5SWA0 Q2, 5LWF0 Q3)
 - Magnetism and Torque production
 - Electric and Magnetic Circuits → Break!
 - Synchronous permanent magnet (PM) machines
 - Control aspects
 - EM Efficiency/Power loss maps

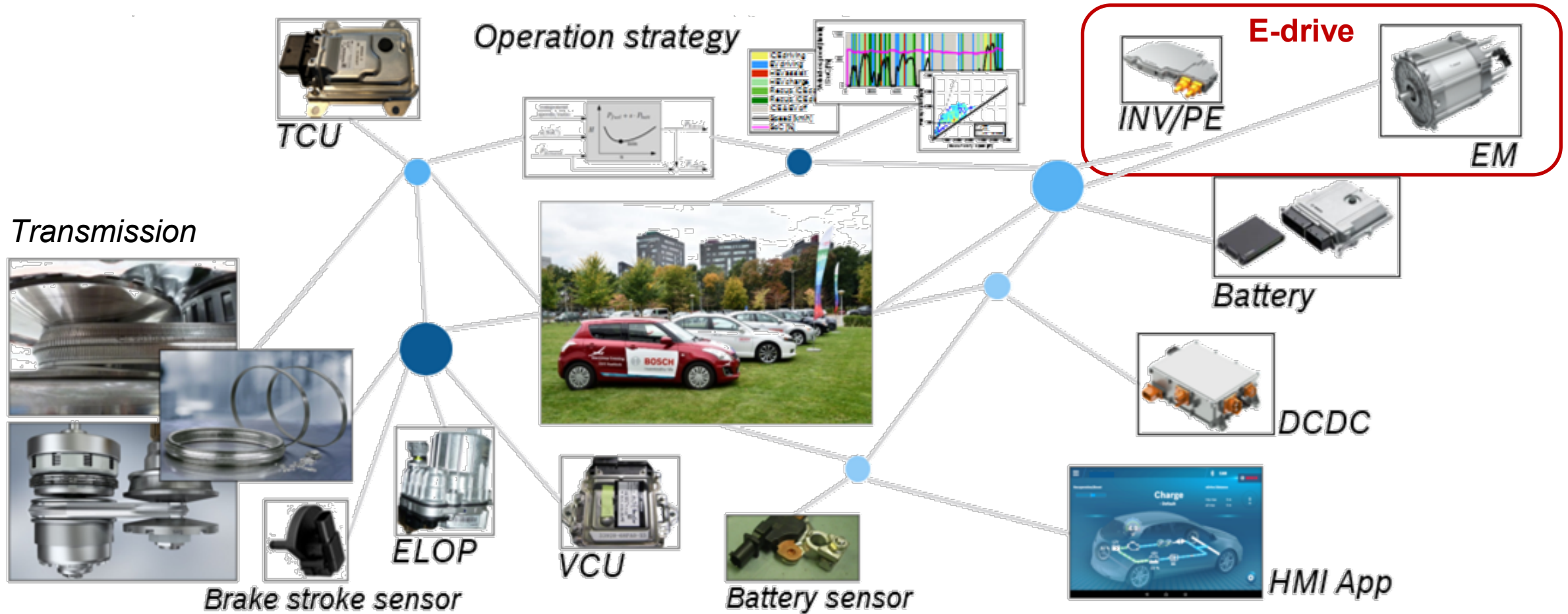
Intended Learning outcomes:

- Identify the main working principles and constraints of the traction E-drives and E-machines
- Explain the basic concept for the E-machine control
- Describe the component-system level interactions

ELECTRICAL DRIVES (E-Drives)

Automotive as an inter-connected system

5

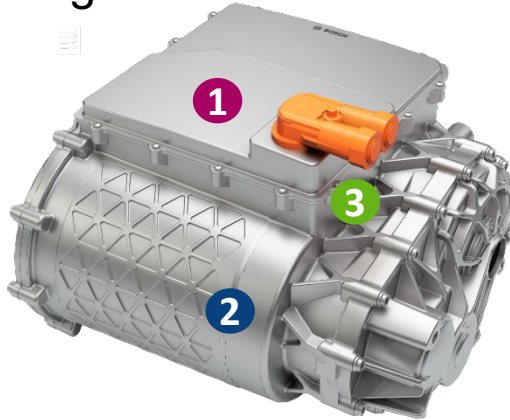


EM: Electrical machine, INV: Inverter, PE: Power Electronics, TCU: Transmission control unit, VCU: Vehicle control unit, ELOP: Electrical oil pump, HMI: Human machine interface

Examples of system integration – eAxle

6

Source: Bosch eAxle for passenger vehicles



1

Direct integrated power electronic

Reduction of cost, weight & losses

2

One shared bearing shield for E-machine & Transmission

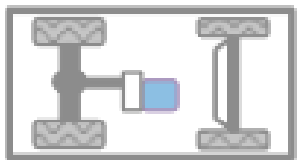
Reduction of cost & weight

3

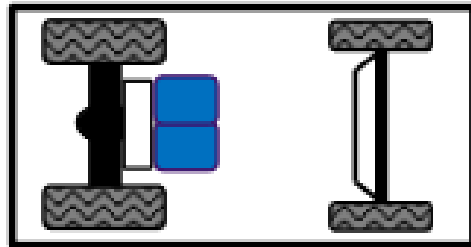
One common cooling circuit for power electronics & e-machine

Reduction of interfaces

Topology scaling in Commercial Vehicles
(heavy-duty applications)



Central Drive



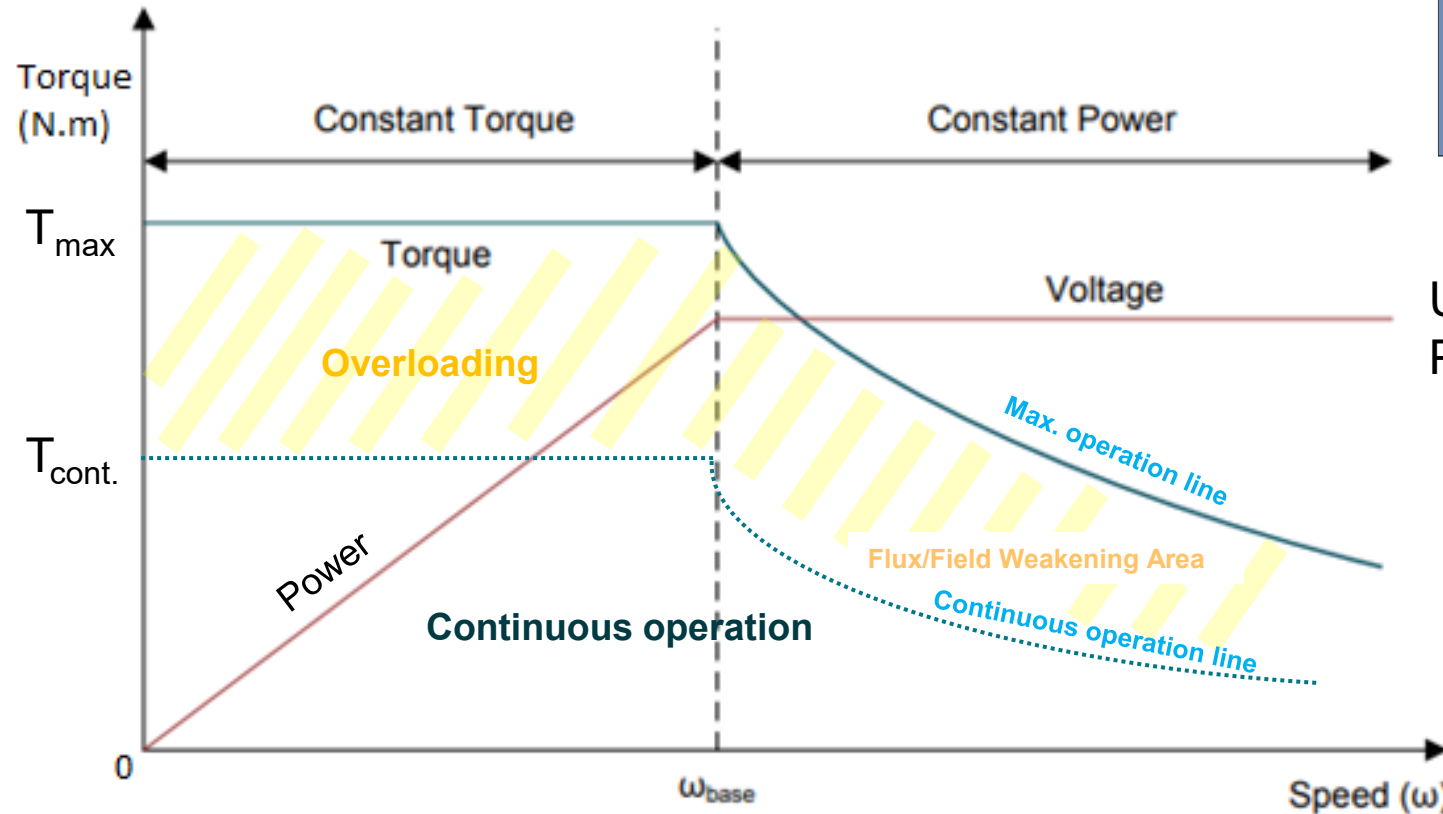
Rigid e-Axle

Main challenge is:

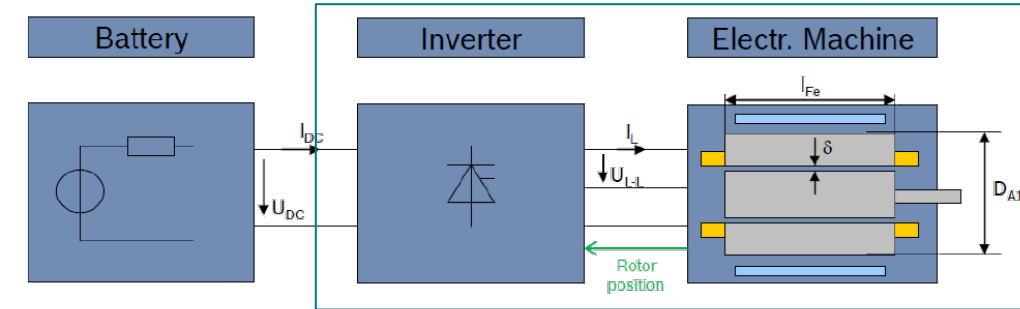
- Improved Motor Cooling (air+water) for better higher power/ better performance

EM & E-drive operation modes & terminologies

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IDEALIZED CURVES

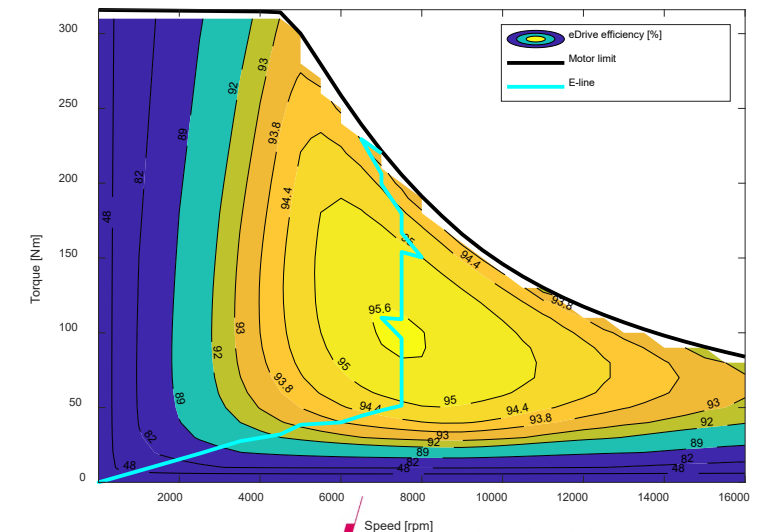


EM + INV = E-Drive / EDR

$$U_{max} < U_{DC}$$

$$P_{max}$$

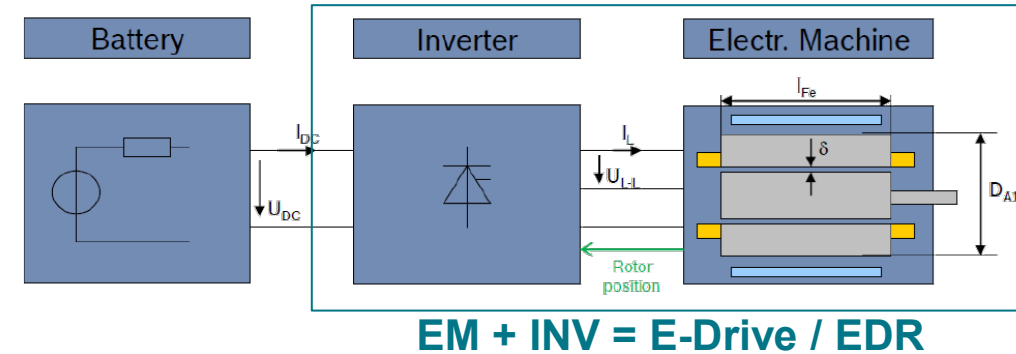
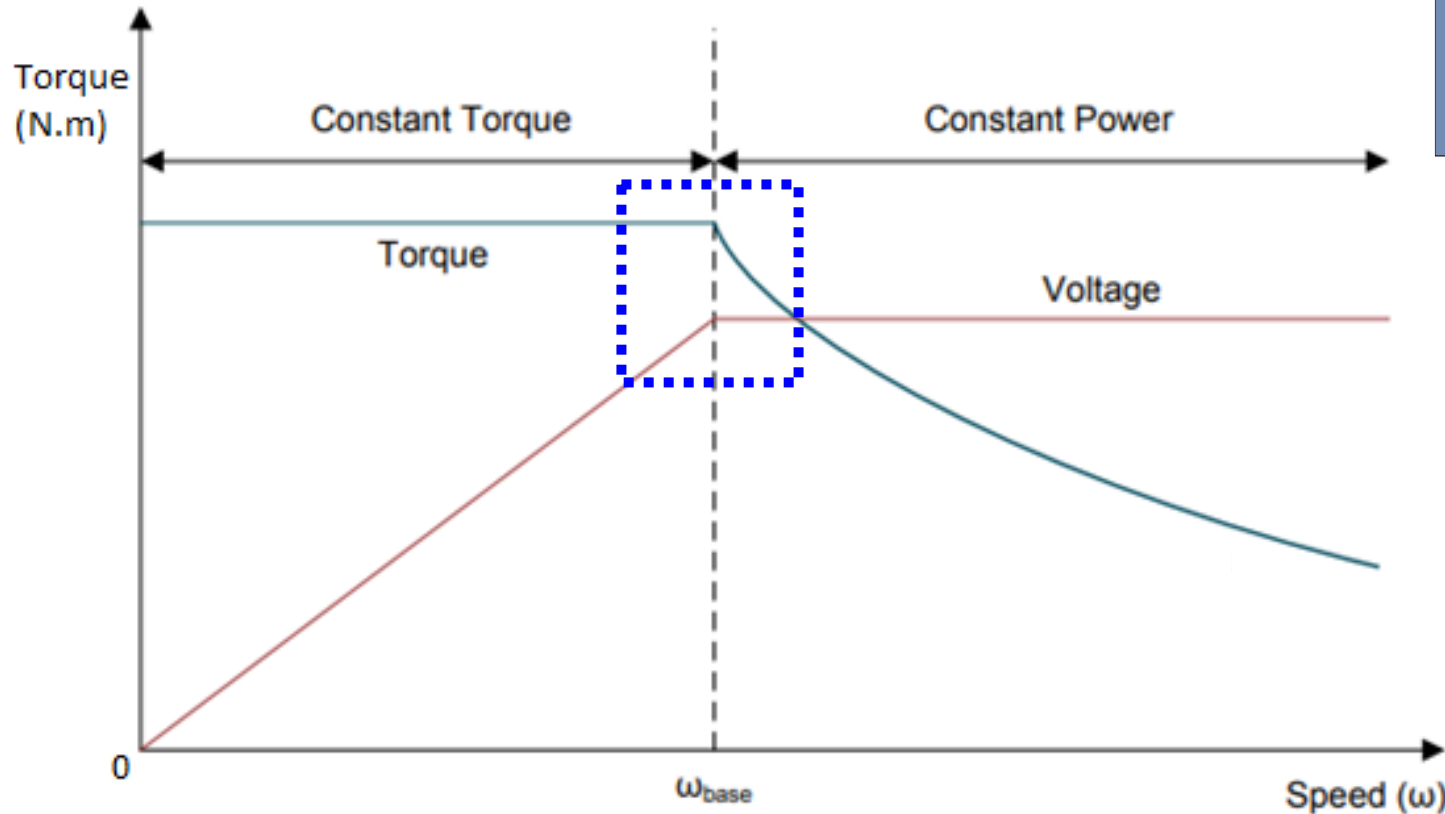
Efficiency / Power loss map



Important performance parameter: Cont-peak power ratios

EM & E-drive operation modes & terminologies

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Corner point @base speed:

- Performance limited by allowed max. current (Torque) & max. voltage (Power),
- Control strategy changes
- Control strategy directly affects torque (torque control)
- The base speed definition can change if target is to maintain “max torque” or “max power”.
- Where the actual “max” power & “max” torque are located can shift around the base speed.

Idealized curves, Definitions can change depending on control strategies!

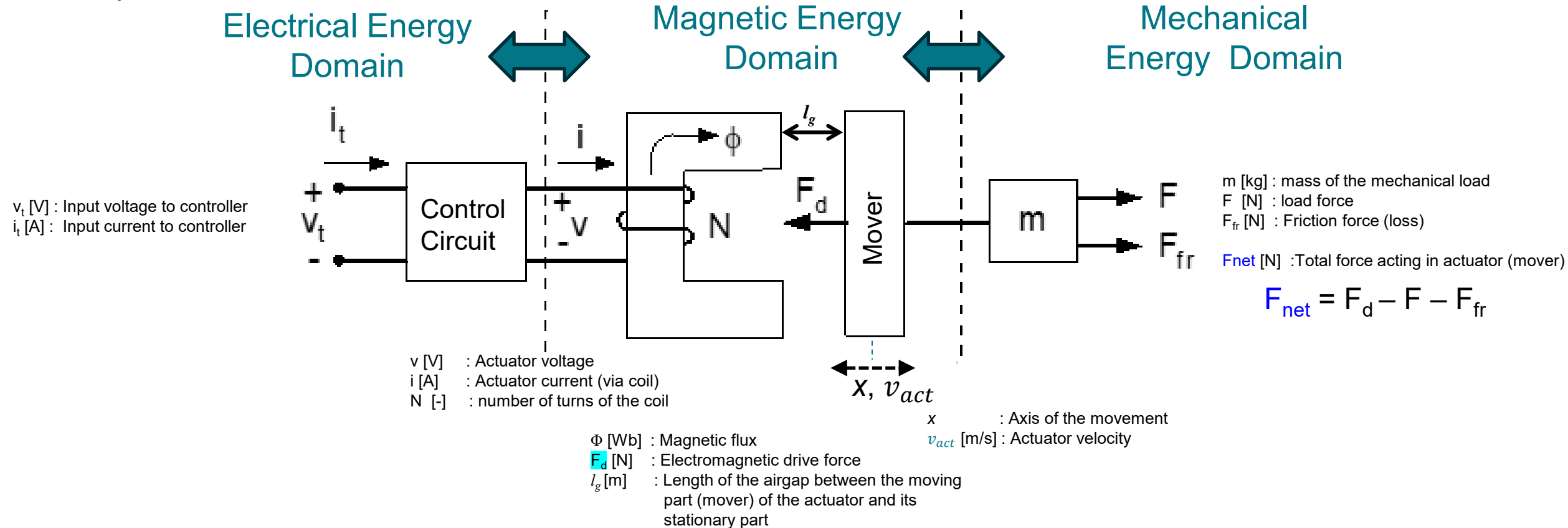
Electrical Machines (EM)

(Magnetism & Torque production)

Electromechanical Energy Conversion

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- Multi-physical domain operation
- Example: An actuator



If no internal losses $\rightarrow P_{el} = P_{mech}$

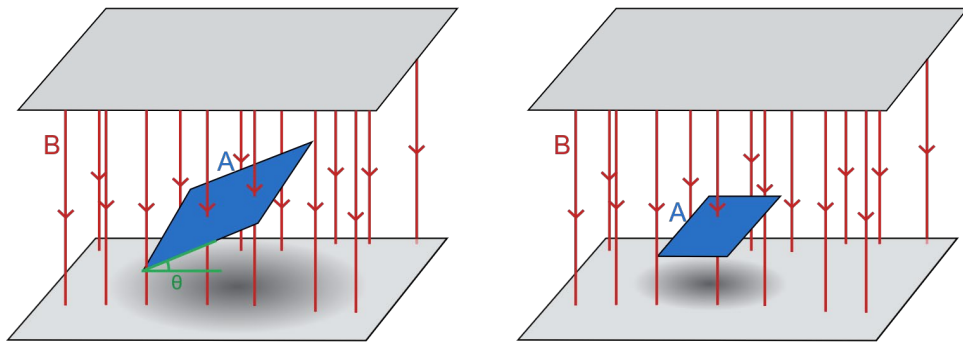
$$v_t * i_t = v * i = F_{net} * v_{act} = T_{net} * w_{act}$$

T_{net} [Nm] : Net torque
 w_{act} [rad/s] : Actuator angular velocity

Magnetic Flux (Φ) and Magnetic Flux Density (B)

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Magnetic flux Φ is a measurement of the total magnetic field



$$\Phi = B \cdot A \cdot \cos \theta$$

$$\lambda = n \cdot \Phi$$

Where:

Φ : Magnetic Flux (Linkage) [Wb, Weber]

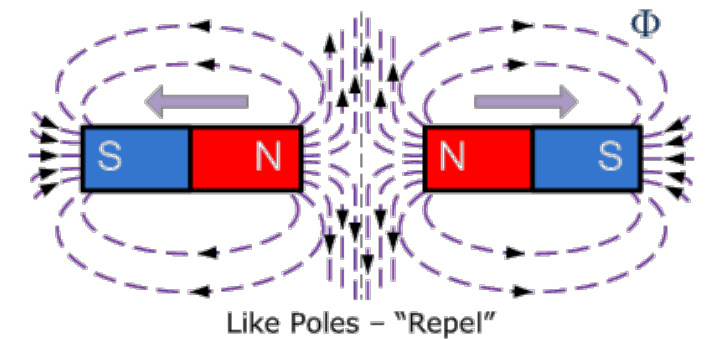
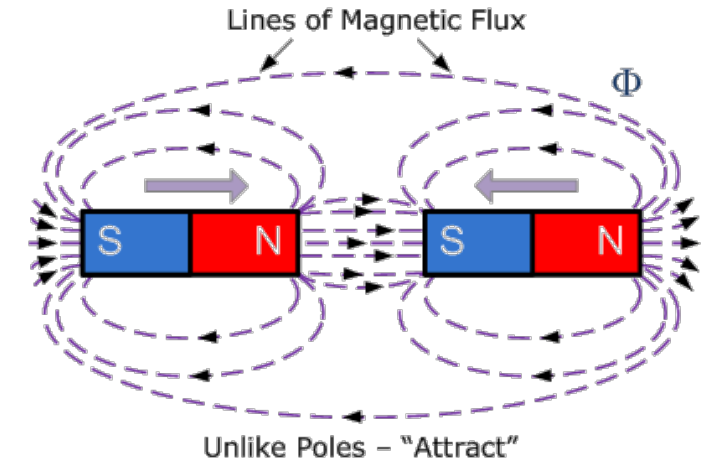
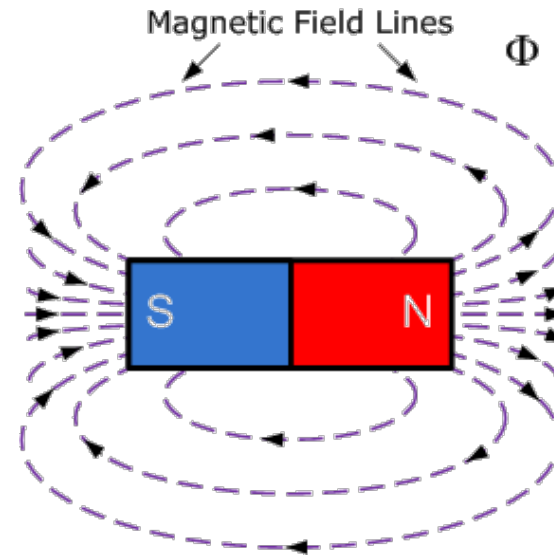
λ : Magnetic Flux Linkage [Weber-turns]

B: Magnetic Flux Density (Magnitude of the magnetic field) [Wb/m^2 or Tesla]

A: Area of surface [m^2]

θ : Angle between the magnetic field lines and the normal (perpendicular) to A [$^\circ$ or Degree].

n: number of turns of coil / conductor



EMs are constructed of

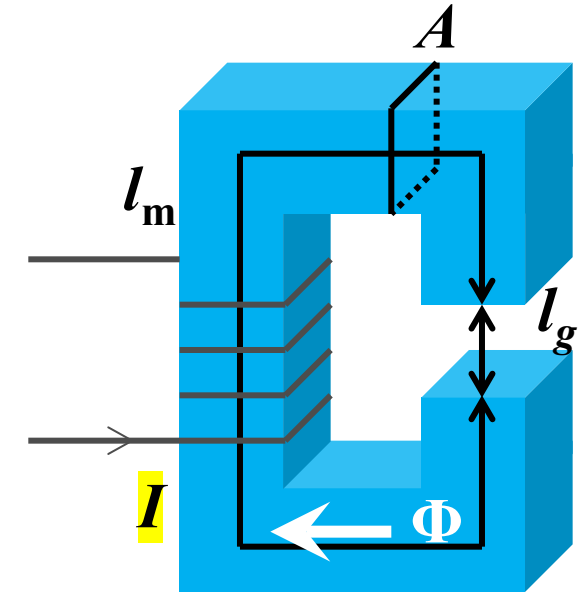
1. **(Magnetic) Field sources (Φ) :**

- conductors, coils (copper, aluminum, etc.) carrying current I
- magnets (permanent magnet (PM) as rare-earth (NdFeB, SmCo), ferrite, etc.)

2. **(Soft) Ferromagnetic materials (l_m):** affected / magnetized by external magnetic field and provides flux paths (increases energy density in the device/EM)

- Iron (core) with Silicon (SiFe), with cobalt (CoFe), with Nickel (NiFe)

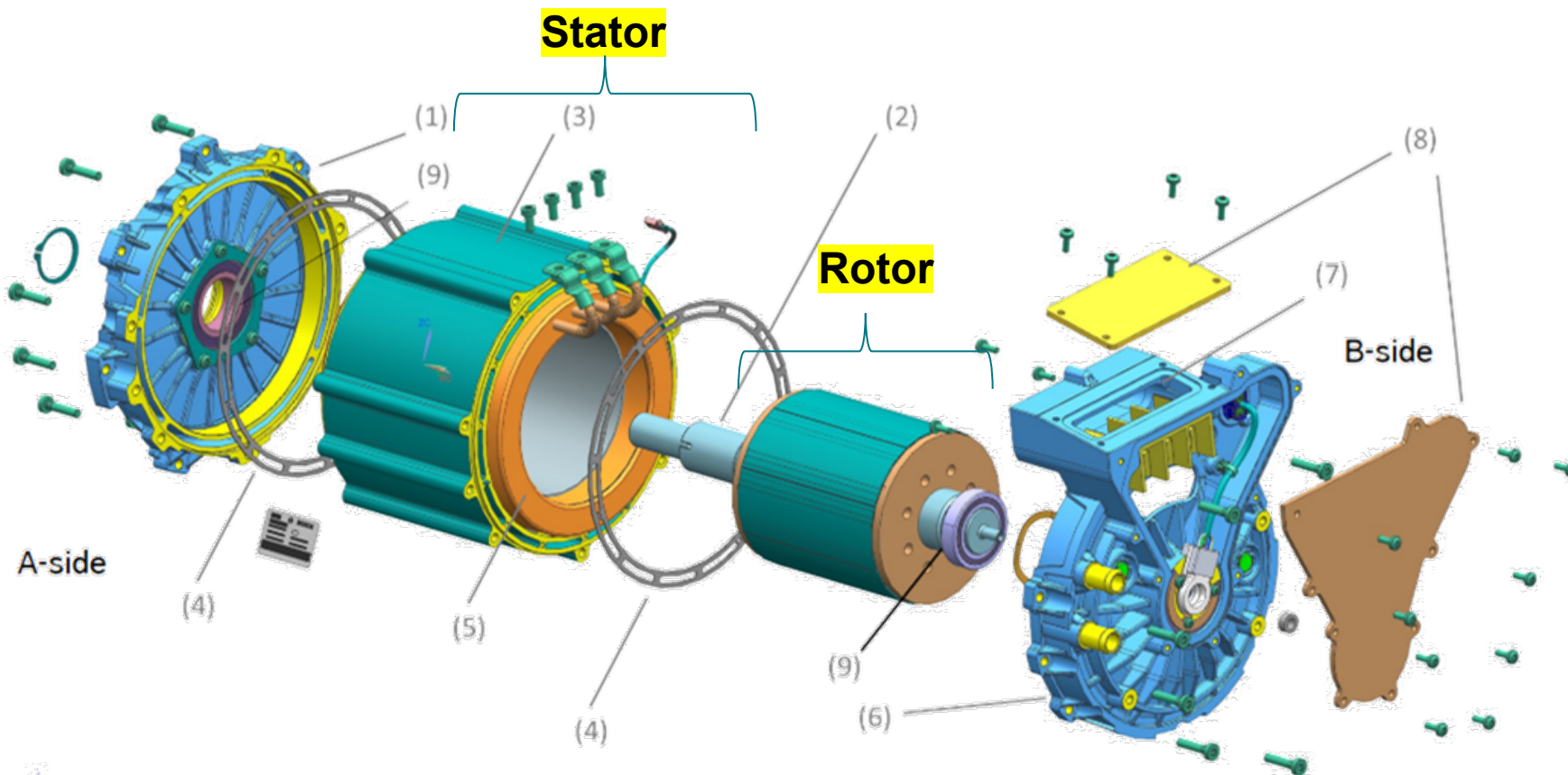
3. **Air (l_g):** medium/airgap where energy conversion takes place (electrical energy $\leftrightarrow$ magnetic energy)



NdFeB: Neodymium Iron Boron
SmCo : Samarium Cobalt

Traction EM: Typical parts

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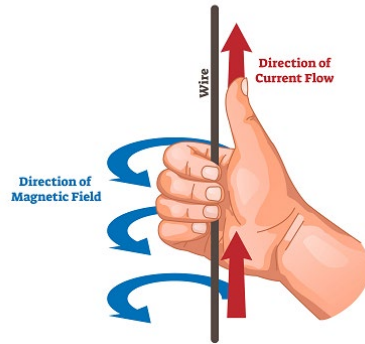
1. End shield A-side
2. Shaft end
3. Housing
4. Sealing

5. Stator winding
6. End shield B-side
7. Terminal box
8. Cover of terminal box
9. Bearing

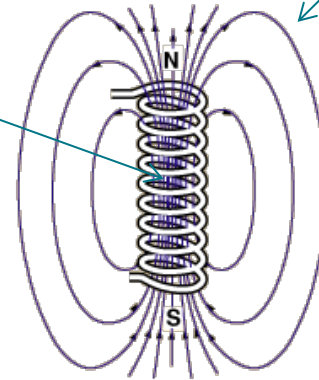
Field sources: Coils or Magnets

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CURL RIGHT HAND RULE

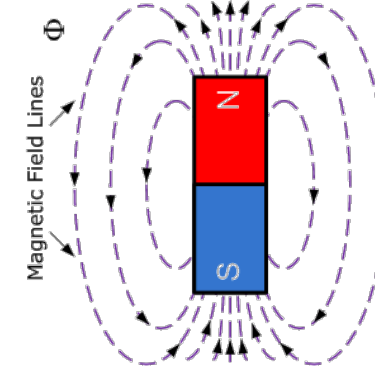


Current
Carrying
Coil / conductor



Electromagnet

Magnetic field
(flux) lines

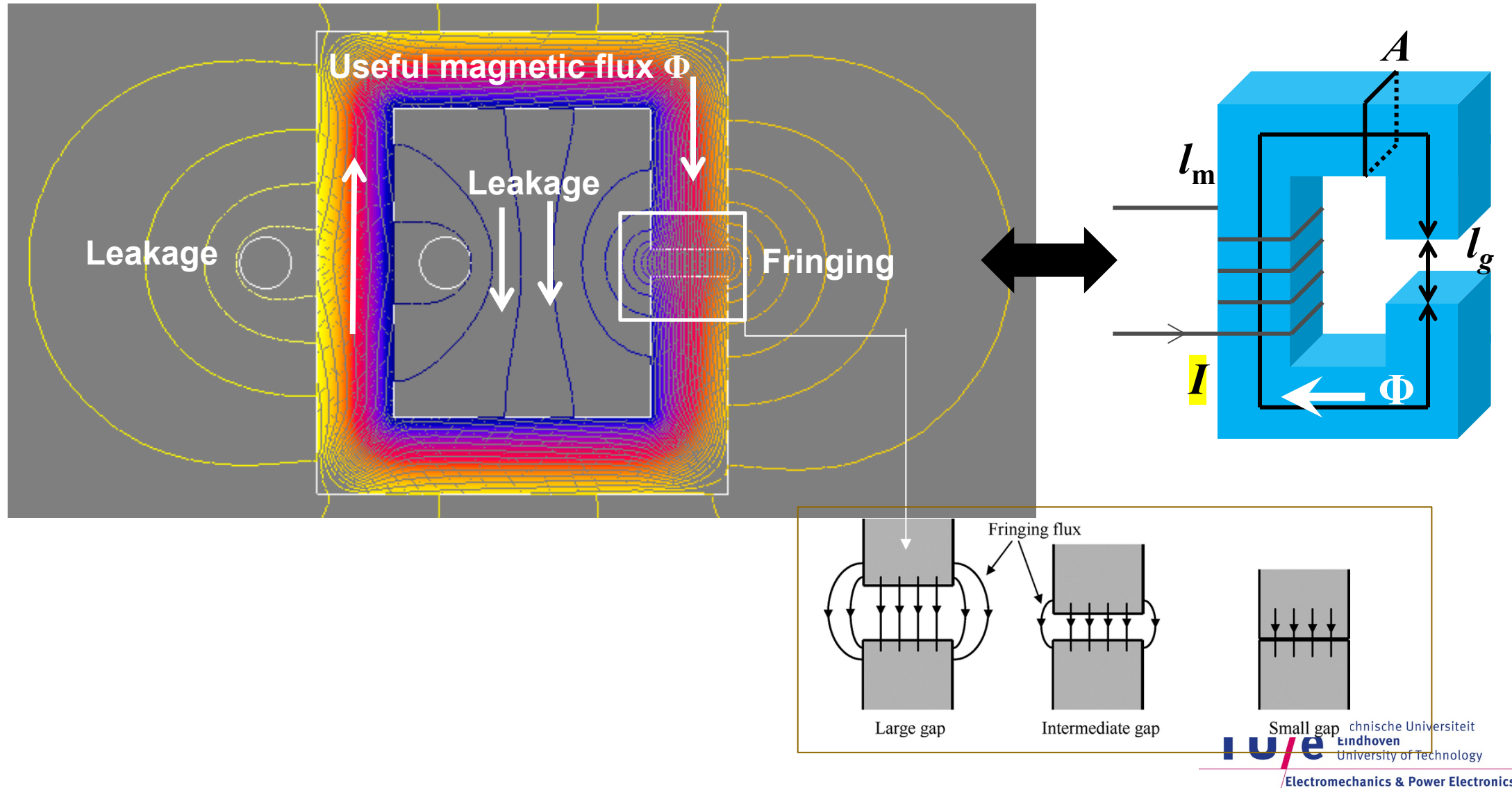


(Permanent) Magnet

EM with...	Coils	Magnet
Torque capability	Moderate	High
Efficiency	Moderate	High
Operational speed range	High (limited by thermal insulation of coil)	Low/moderate (limited by demagnetization)

Magnetic flux in ferromagnetic (iron) material

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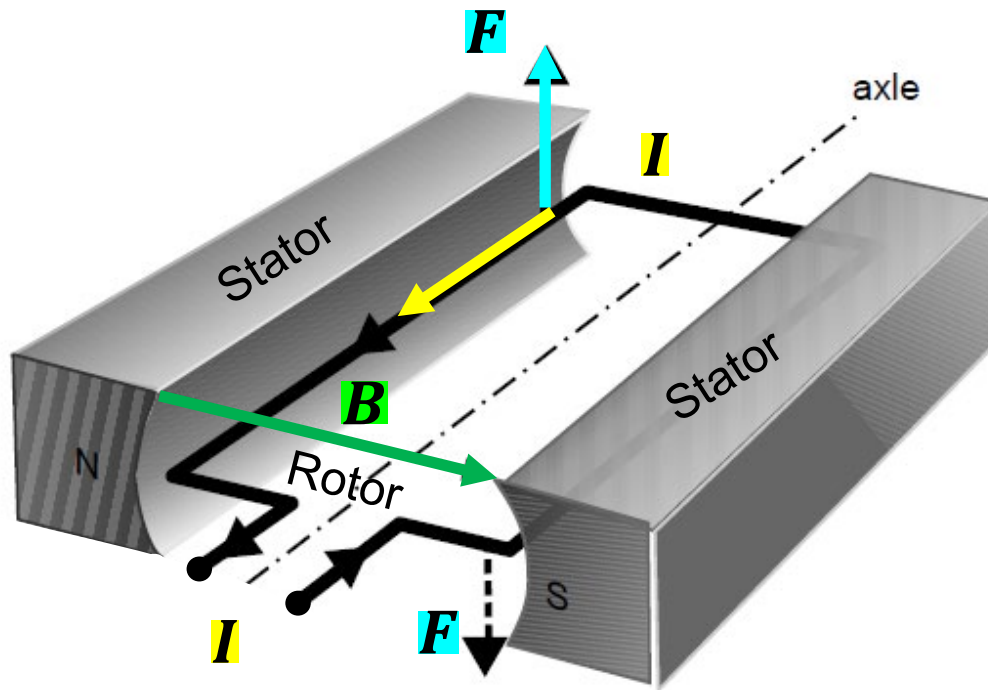


Torque production mechanism: Lorentz force

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Example: Simplified DC Motor:

- Rotor: 1 coil conductor (wire) carrying current I
- Stator: 1 magnetic pole pair (1PM with N-S) producing B



• **Physical Law:** A force acts on a current (I) carrying conductor (coil) inside an external magnetic field B

$$F \sim I \times B$$

- B is the (stator) magnetic flux density [Wb m^{-2}]
- I is the (rotor armature) current [A]
- F is the Lorentz force [N]

Lorentz Torque

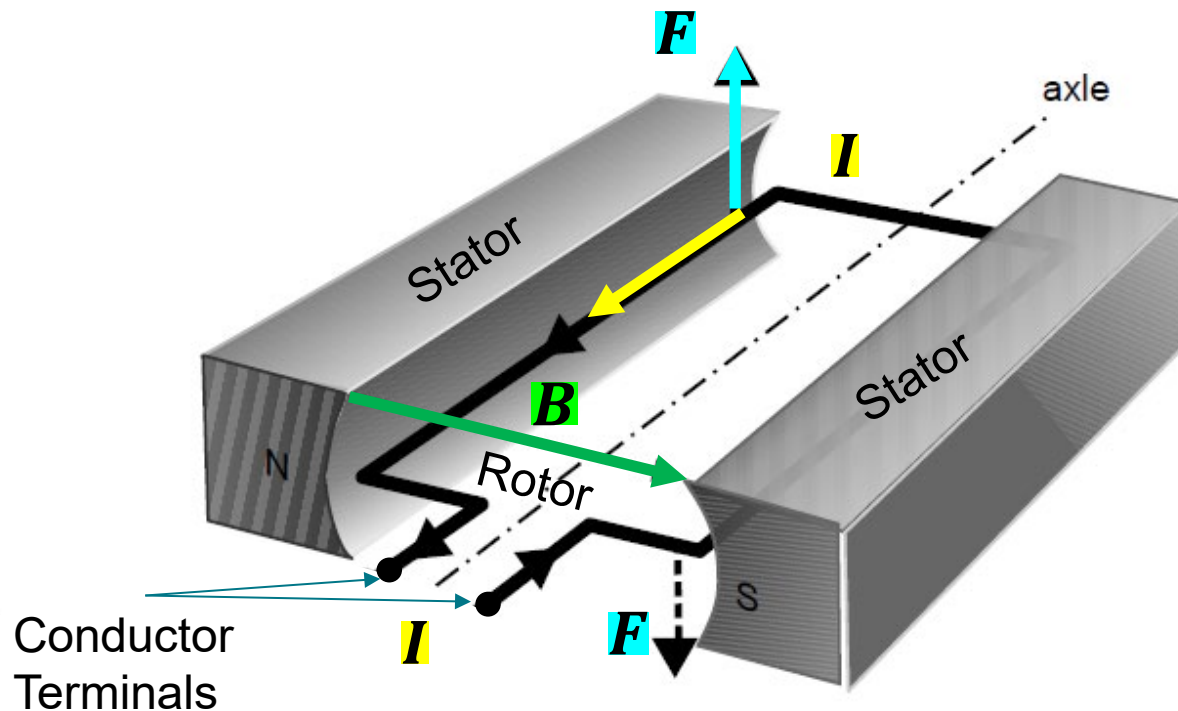
$$\begin{aligned} \rightarrow T &\sim I \times B \quad \text{OR} \\ \rightarrow T &\sim I \times \phi \quad \text{OR} \\ \rightarrow T &\sim I \times \lambda \end{aligned}$$

Torque production mechanism: back-EMF

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Example: Simplified DC Motor:

- Rotor: 1 coil conductor (wire) carrying current I
- Stator: 1 magnetic pole pair (1PM with N-S) producing B



• **Physical Law***: Movement (speed v) of conductors (rotor winding) in an external magnetic field (stator magnetic field B) generates a voltage drop at its (rotor) terminals, i.e. back-EMF**

$$e_b \sim B v$$

$$e_b \sim \phi \omega$$

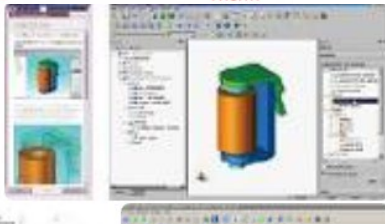
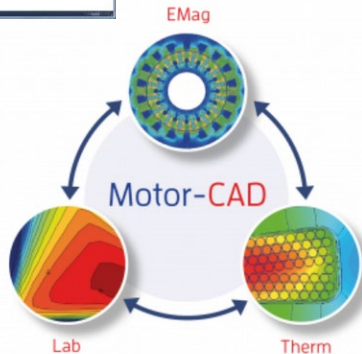
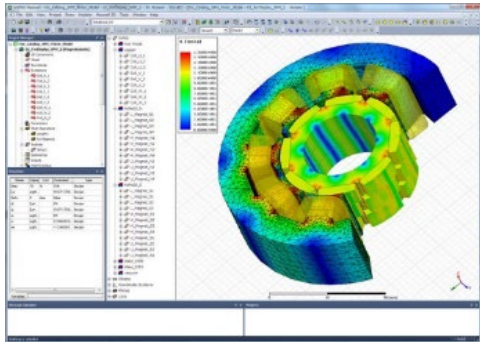
Note: Excitation/magnetic field B responsible for E_b can be created by magnets (PM) or current carrying conductor

*Faraday and Lenz laws, ** EMF: Electro-motive force

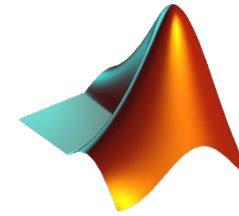
Electrical Machines (EM)

(Electric and Magnetic Circuits)

Numerical approaches



Analytical approaches

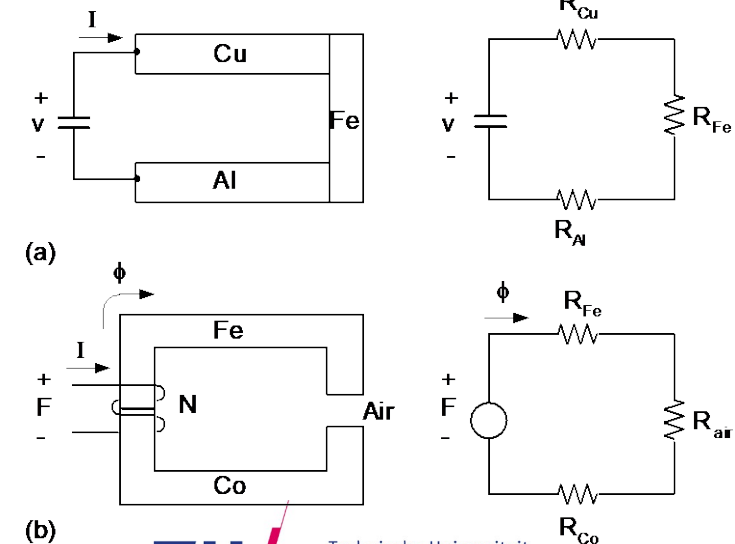


MATLAB

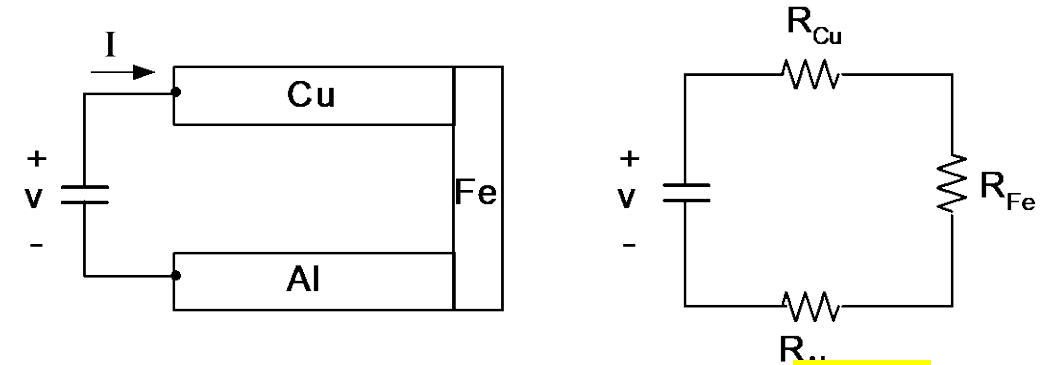
Harmonic series expansions



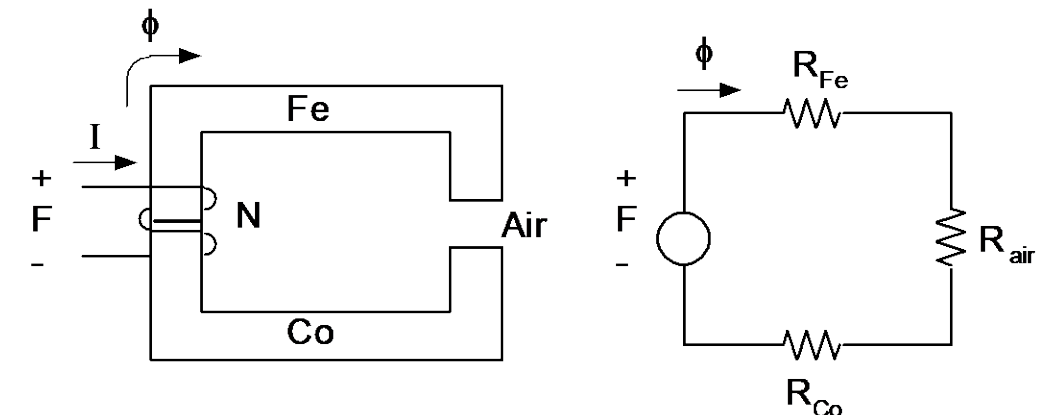
Equivalent circuits



Electric		Magnetic	
Voltage	V (V)	MMF	F (A-t)
Current	I (A)	Flux (linkage)	ϕ * (or λ) (Wb)
Resistance	R (Ω)	Reluctance	R (H^{-1})



(a) **Electrical domain:** Direct and indirect electrical field sources are represented by voltage supply and electrical resistances of the used wires (Copper & Aluminum)



(b) **Magnetic domain:** Ferromagnetic core (Iron or Cobalt) shows a similar resistance to the magnetic field sources.

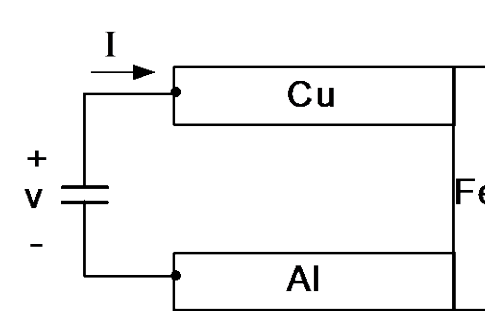
Note: An example indirect voltage source is the E_b back-EMF.

Analogy between electric and magnetic circuits

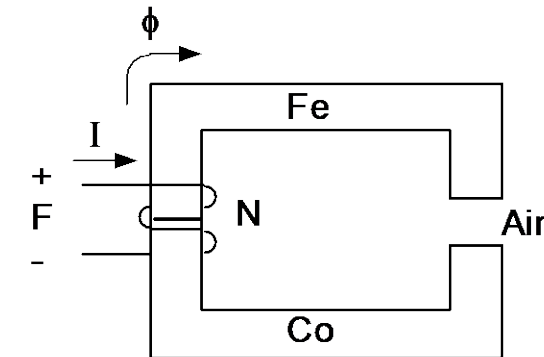
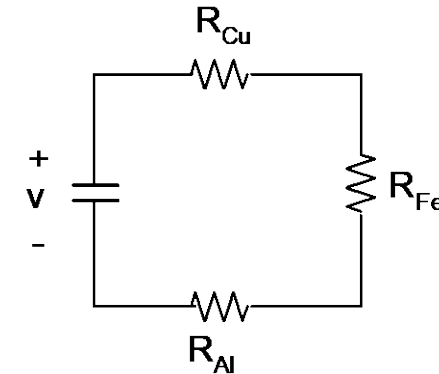
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Electric		Magnetic	
Voltage	V (V)	MMF	F (A-t)
Current	I (A)	Flux (linkage)	ϕ^* (or λ) (Wb)
Resistance	R (Ω)	Reluctance	R (H^{-1})
Conductance	G (S)	Permeance	P (H)
Electric field intensity	E (V/m)	Magnetic field intensity	H (A-t/m)
Current density	J (A/m ²)	Magnetic flux density	B (T OR Wb/m ²)
Conductivity	σ (S/m)	Permeability	μ (H/m)
$V = IR$ $J = \sigma E$ $R = \frac{l}{\sigma A} = \frac{1}{G}$		$F = \phi R$ $B = \mu H$ $R = \frac{l}{\mu A} = \frac{1}{P}$	

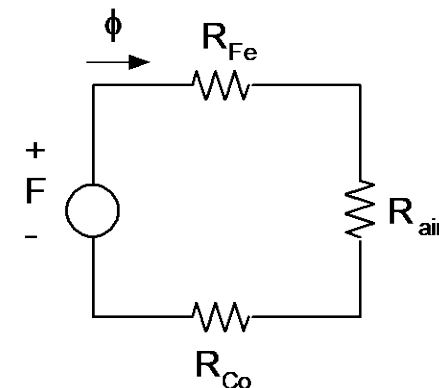
$$L = \frac{d\lambda}{di} = n \frac{d\phi}{di} = n \frac{dB \times A}{di}$$



(a) **Electric circuit** (Copper & Aluminium are typically used in windings)

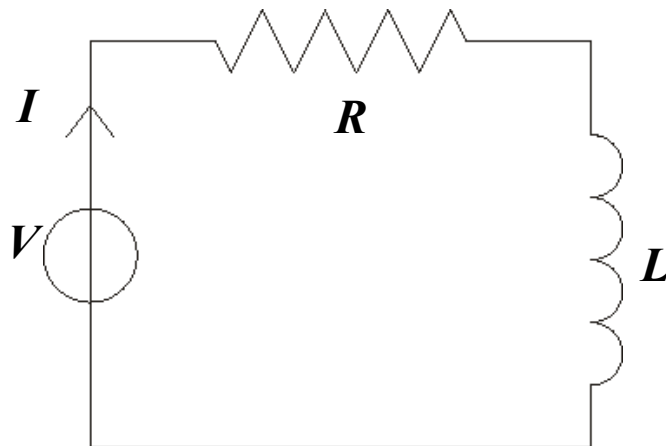


(b) **Magnetic circuit** (Iron & Cobalt are typically used in ferromagnetic core)



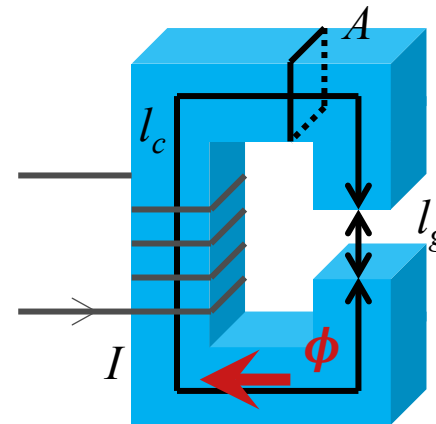
- The **inductance** (or coil) is an electric circuit variable that relates the magnetic field variable (**flux linkage λ**) to the electric circuit variable (**current i**).

Electric circuit



$$V = IR + L \frac{di}{dt}$$

Magnetic circuit



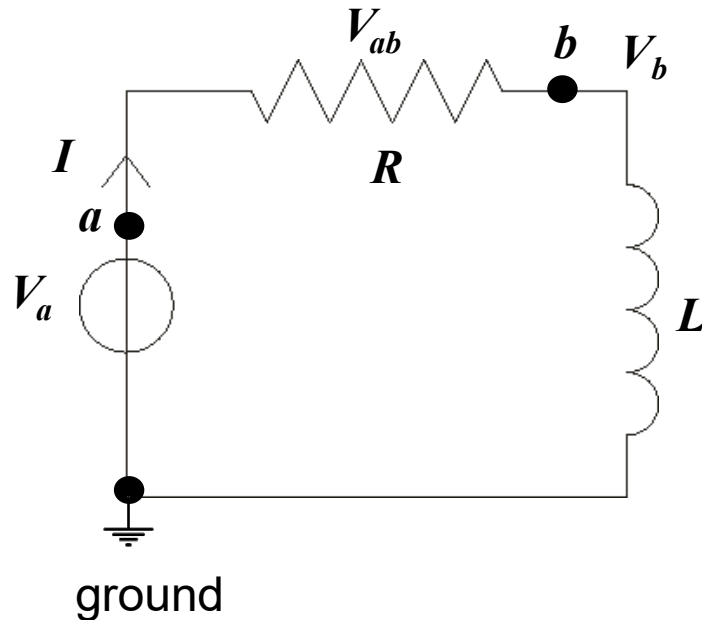
$$L = \frac{d\lambda}{di} = n \frac{d\phi}{di} = n \frac{dB \times A}{di}$$

R [ohm] : wire resistance
 L [Henry] : the wire inductance
 n [-] : number of turns
 A [m²] : effective area where the magnetic flux ϕ passes

Note: In the EM circuit representation, winding-cables are represented by series connected R-L.

Voltages:

- V_a is the voltage of node a with respect to ground
- $V_{ab} = V_a - V_b$ refers to the voltage of node a with respect to node b



Source: V_a

Load: R-L,

$$V_{ab} = V_R = I R,$$

$$V_b = V_L = L \, di/dt$$

Typical Representation:

Lowercase letters (e.g. i): instantaneous value (time depending quantity)

Uppercase letters (e.g. I): average or RMS values

Electric circuits: AC signals (time-dependent), RMS (effective) voltage and current

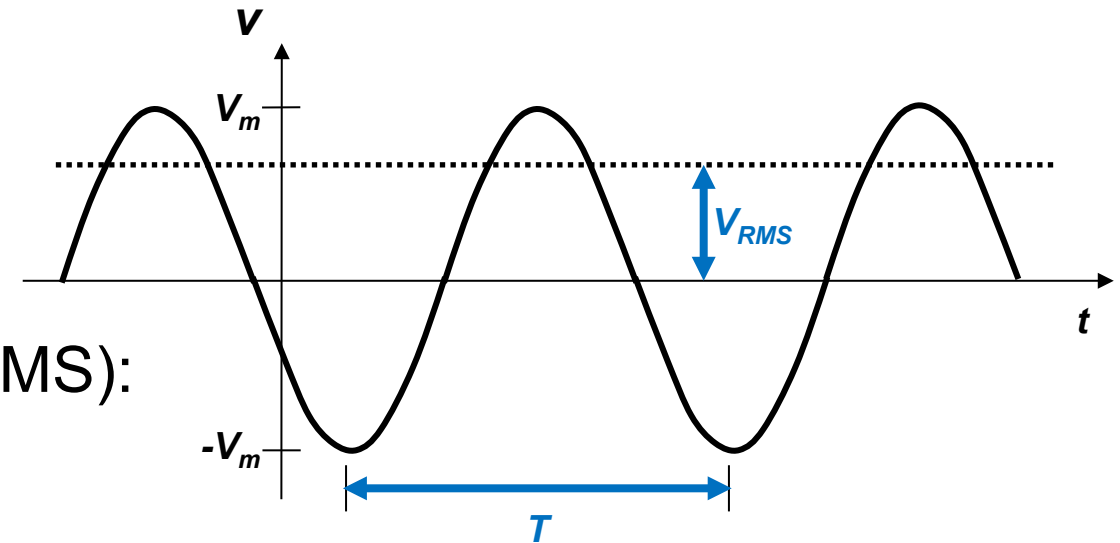
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- Example: Sinusoidal voltage $v(t)$:

$$v(t) = V_m \cos(\omega t + \phi)$$

- Apply definition of Root-Mean-Square (RMS):

$$V = \sqrt{\frac{1}{T} \int_{t_1}^{t_1+T} v^2(t) dt}$$
$$V_{RMS} = \frac{1}{\sqrt{2}} V_m$$



Electrical period / cycle [s] : T

Electrical frequency f [Hz]: $f = 1/T$

Electrical speed ω [rad/s]: $\omega = 2\pi f$

Time: t

- If $v(t)$ is non-sinusoidal, the RMS value V can/will be different!
- RMS: equivalent voltage/current for AC, giving same power calculation as for DC (mean, average...)

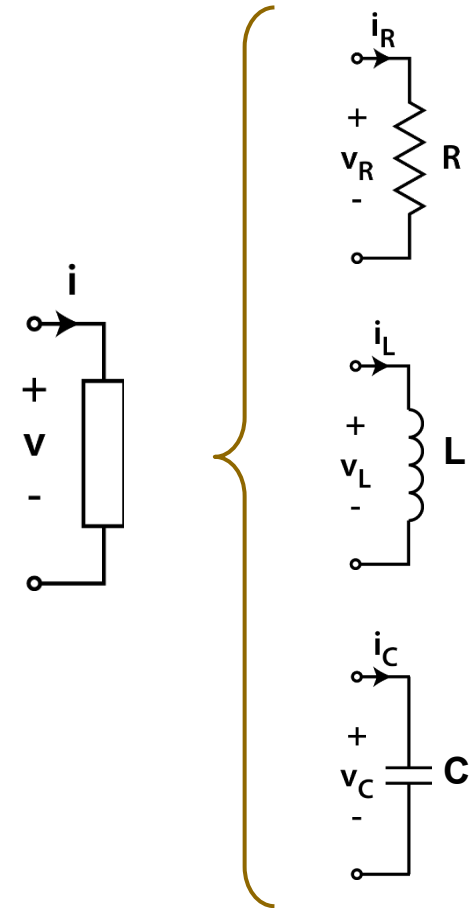
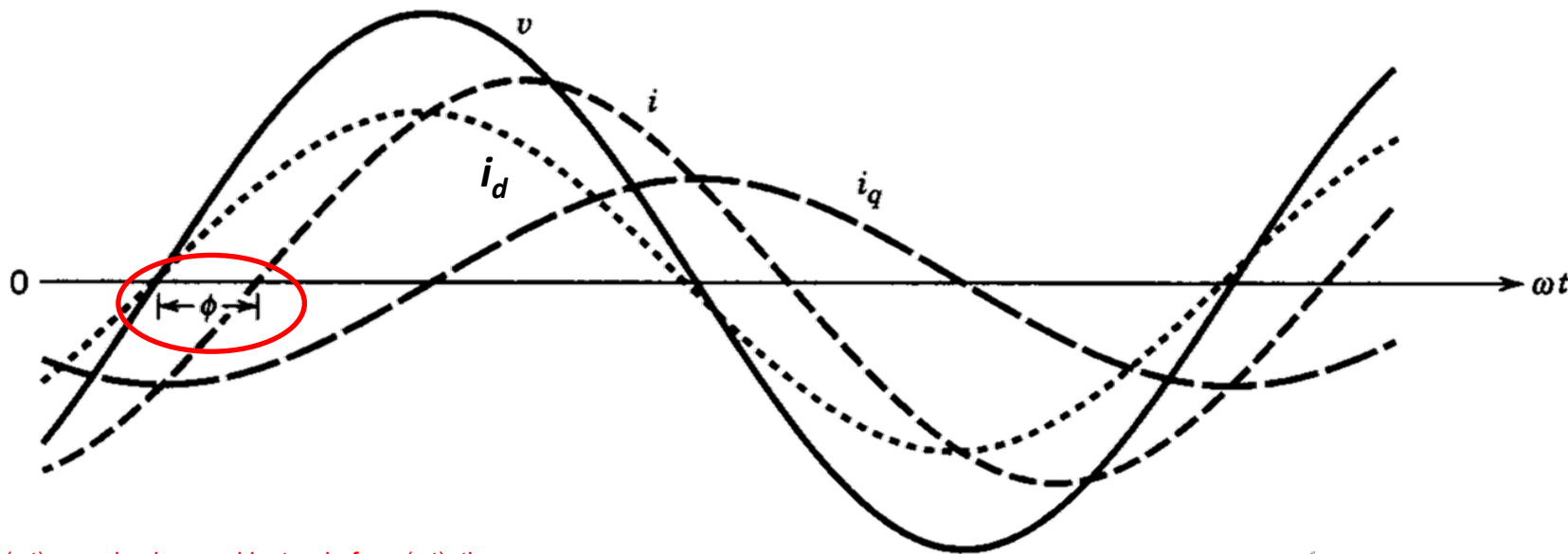
Note: EM electrical speed [rad/s] $\omega_{ele} = p * \omega_{mech}$, where $p[-]$ is EM pole pair number,
 ω_{mech} [rad/s] is EM mechanical speed

Electric circuits:

AC current (i) and AC voltage (v)

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- Sinusoidal steady-state condition
 - Linear systems (v,i) do not change in frequency, but only in amplitude & phase
 - If EM speed changes $\rightarrow$ frequency also changes ($\omega = 2\pi f$)
- Electrical loads can be ...
 - Resistive load (v & i in same phase)
 - Inductive load (v & i not in same phase, **phase shift ϕ**)
 - Capacitive load (v & i not in same phase, phase shift) $\rightarrow$ Not used in EM modeling

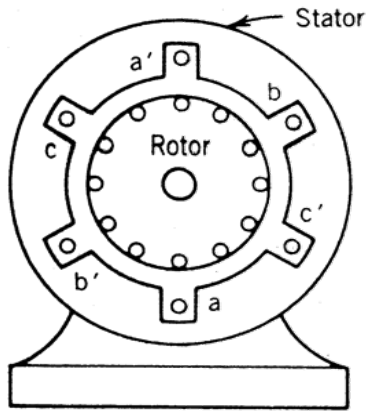


Note: $\sin(\omega t)$ can also be used instead of $\cos(\omega t)$, they are both sinusoidal functions!

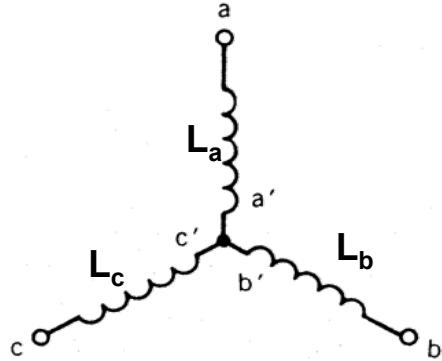
Electric circuits: Multi-phase current and voltages

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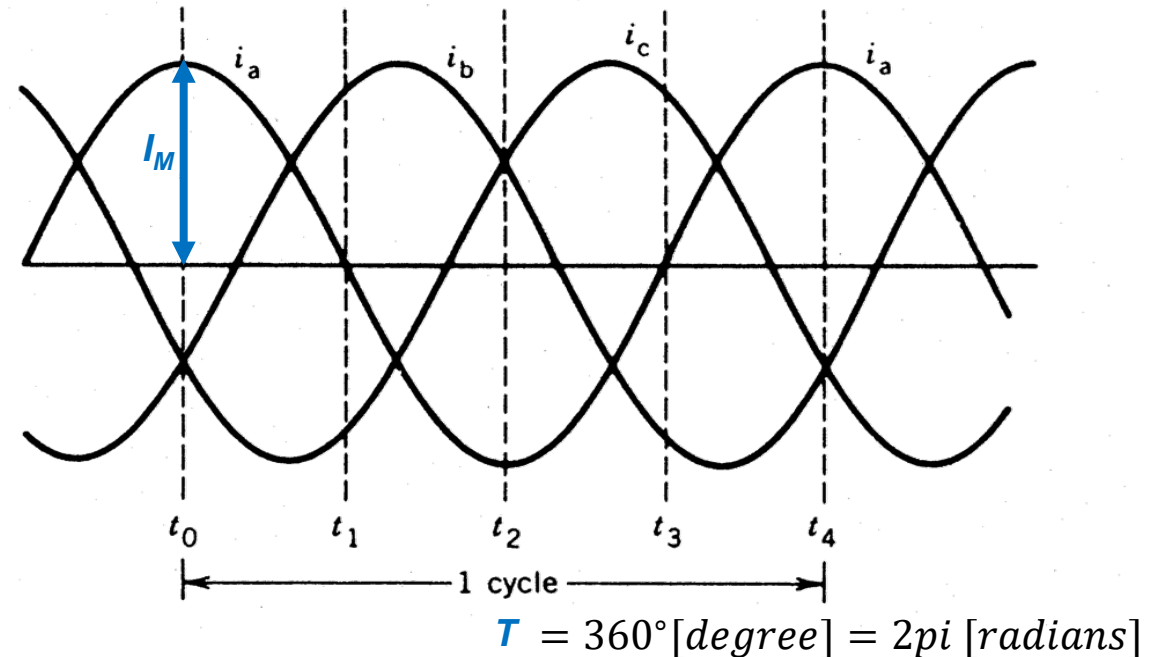
Example: 3-phase systems



Cross-sectional view of EM



Stator windings with **3-phase** currents i_a , i_b and i_c



$$\begin{aligned}i_a &= I_m \cos \omega t \\i_b &= I_m \cos(\omega t - 120^\circ) \\i_c &= I_m \cos(\omega t + 120^\circ)\end{aligned}$$

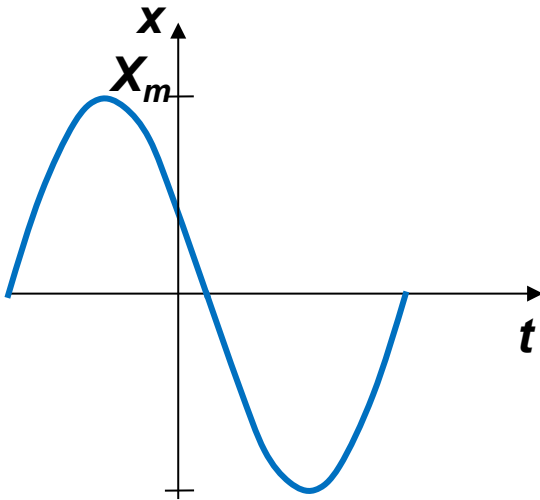
At a given time :

$$i_a + i_b + i_c = 0 \rightarrow \text{Balanced system}$$

$$\begin{aligned}i_a &= I_m(t = t_0 = 0) \\i_b &= -\frac{I_m}{2} \\i_c &= -\frac{I_m}{2}\end{aligned}$$

- Time-dependent signal

$$x(t) = \sqrt{2}X \cos(\omega t + \phi)$$



Waveform $x(t)$:

- Time dependent
- Always real quantity

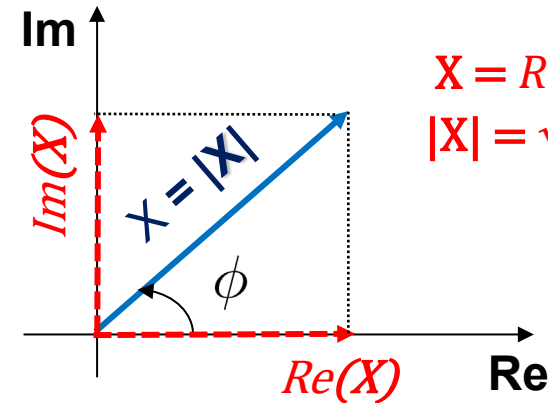
$$v = \sqrt{2}V \cos(\omega t)$$

$$i = \sqrt{2}I \cos(\omega t - \phi)$$

- Phasor representation

$$\mathbf{X} = X e^{j\phi} \quad \mathbf{X} = \bar{\mathbf{X}} = \vec{X}$$

$$x(t) = \sqrt{2} \operatorname{Re}(\mathbf{X} e^{j\omega t})$$



$$\mathbf{X} = \operatorname{Re}(\mathbf{X}) + j \operatorname{Im}(\mathbf{X})$$
$$|\mathbf{X}| = \sqrt{(\operatorname{Re}(\mathbf{X}))^2 + (\operatorname{Im}(\mathbf{X}))^2}$$

Phasor $\mathbf{X}$

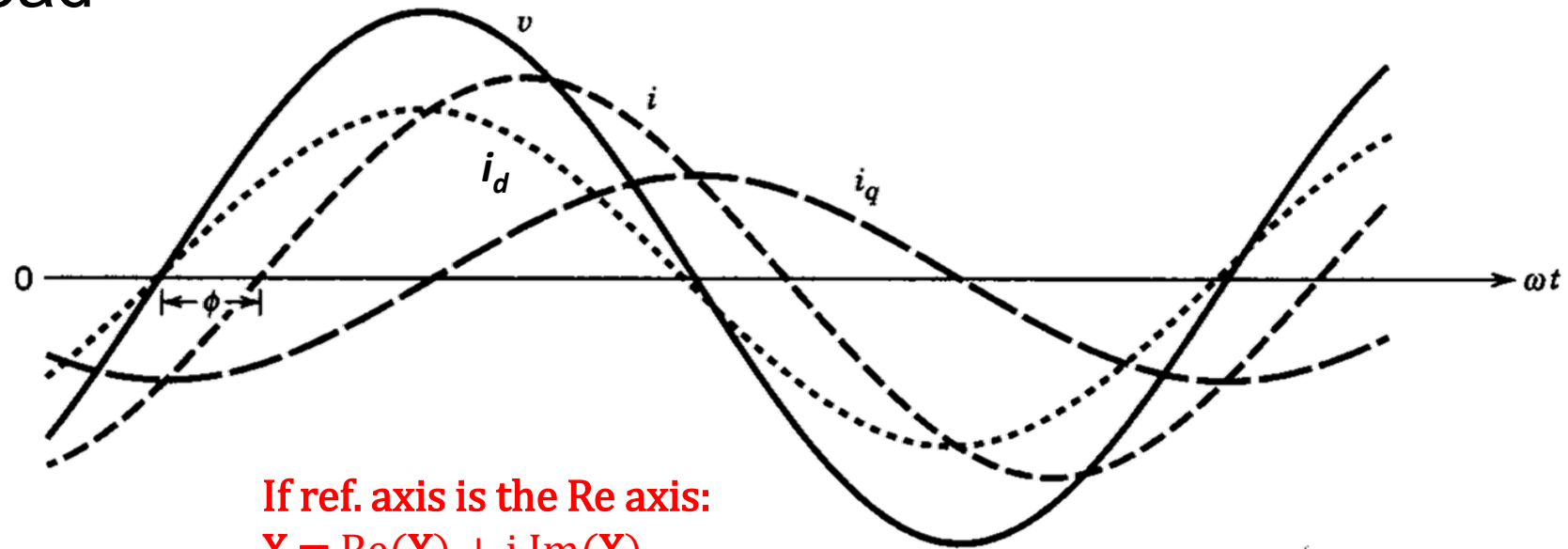
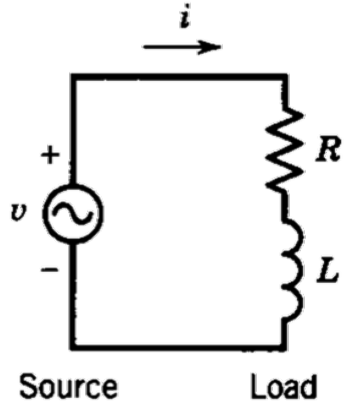
- Time independent
- Complex quantity

Note: $\sin(\omega t)$ can also be used instead of $\cos(\omega t)$, they are both sinusoidal functions!

Electric circuits: Steady-state sinusoidal voltages & currents

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- AC circuit with R-L load

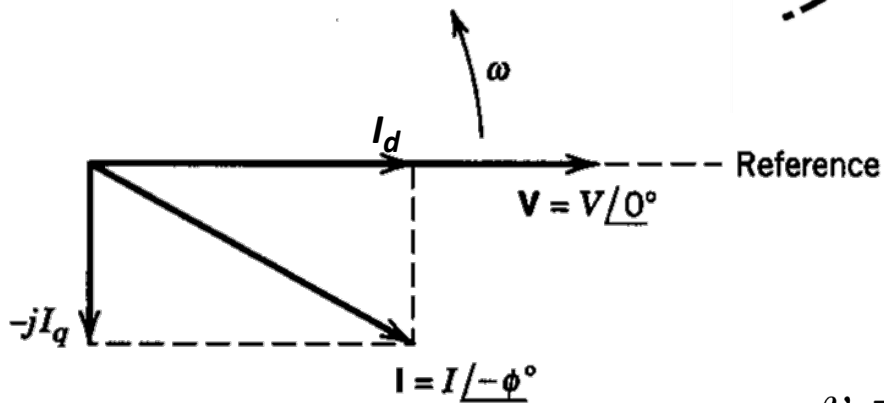


If ref. axis is the Re axis:

$$\mathbf{X} = \text{Re}(\mathbf{X}) + j \text{Im}(\mathbf{X})$$

$$\mathbf{V} = V + j * 0, \quad |\mathbf{V}| = V$$

$$\mathbf{I} = I_d - j * I_q, \quad |\mathbf{I}| = |\mathbf{I}_d - j * I_q| = \sqrt{(I_d^2 + I_q^2)}$$



$$v = \sqrt{2}V \cos(\omega t)$$

$$i = \sqrt{2}I \cos(\omega t - \phi)$$

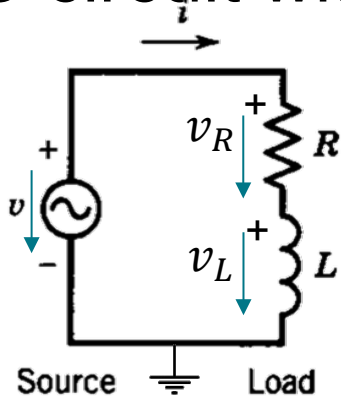
Note: $\sin(\omega t)$ can also be used instead of $\cos(\omega t)$, they are both sinusoidal functions!

Electric circuits: Simulation (Simulink, Simscape, Simscape Electrical)

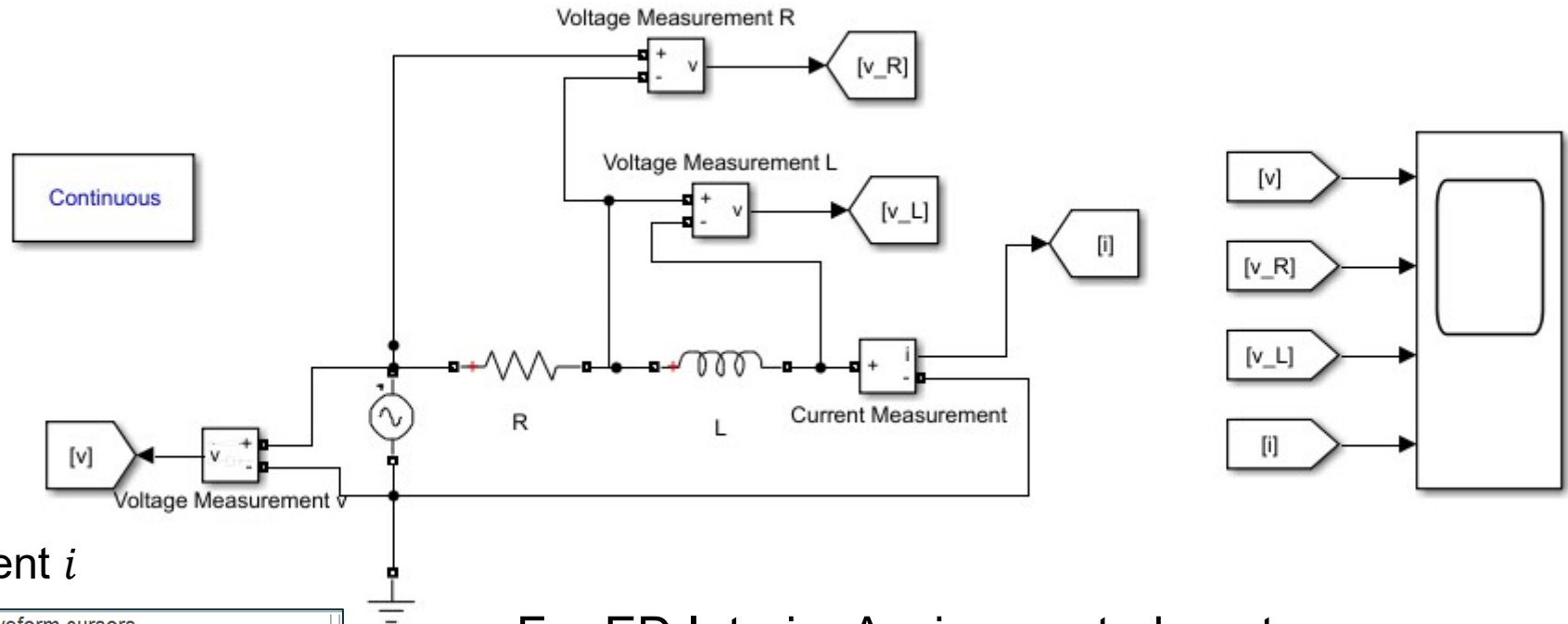
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- AC circuit with R-L load

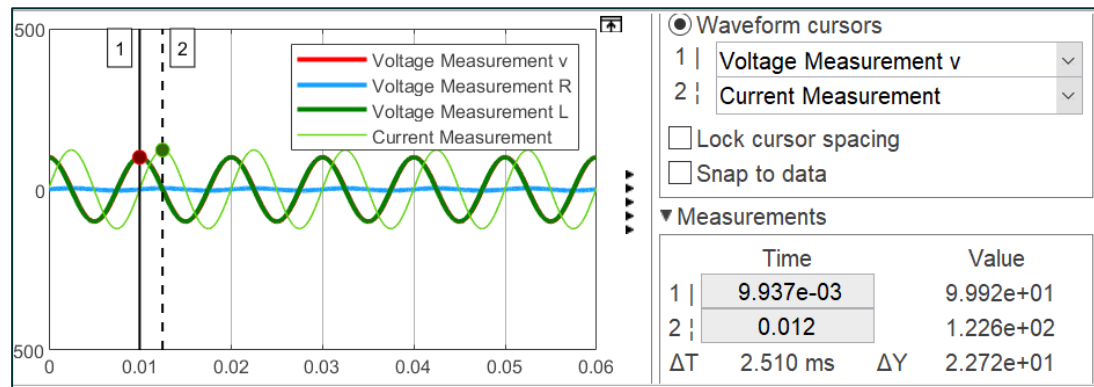
See the example file: RL_circuit_R2023b.slx



$$v(t) = v_R + v_L = Ri(t) + L \frac{di(t)}{dt}$$



Inductor voltage v_L - Current i



For ED Interim Assignment, do not forget to install **Simulink Simscape, Simscape Electrical** packages !

Electrical Power for AC quantities/circuits

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Sinusoidal voltage and current

$$v = \sqrt{2}V \cos(\omega t + \theta_v) \quad \mathbf{V} = V \angle \theta_v$$

$$i = \sqrt{2}I \cos(\omega t + \theta_i) \quad \mathbf{I} = I \angle \theta_i$$

Complex power*

$$\mathbf{S} = \mathbf{V}\mathbf{I}^* = VI \angle (\theta_v - \theta_i) \quad [\text{VA}]$$

$$= P + jQ$$

Apparent power is the length of $\mathbf{S}$

$$S = |\mathbf{S}| = VI = \sqrt{P^2 + Q^2} \quad [\text{VA}]$$

Average (real, active) power

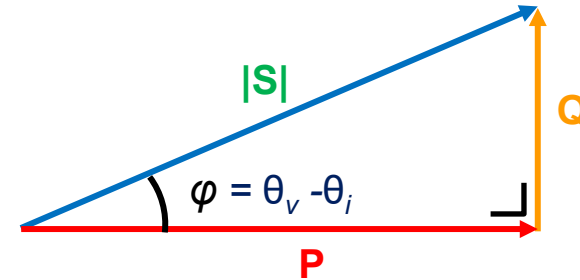
$$P = \text{Re}(\mathbf{S}) \quad [\text{W}]$$

$$= VI \cos(\theta_v - \theta_i)$$

Reactive power accounts for the difference between P and S

$$Q = \sqrt{S^2 - P^2}$$

$$= VI \sin(\theta_v - \theta_i) \quad [\text{VAR}]$$



If we are talking on power flow between powertrain elements of the vehicle (wheel, transmission, etc.), this power is considered !

* Since the considered voltage phasor $\mathbf{V}$ and current phasor $\mathbf{I}$ are sinusoidal the angle difference between them is also the angle φ between P & Q .